

## **Bartenコントラスト感度関数モデルの空間速度拡張 A Spatio-Velocity Extension of Barten's CSF Model**

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2012/3/9

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2011/Dec/7 at Nagoya Convention Center, Japan.  
で発表した内容)

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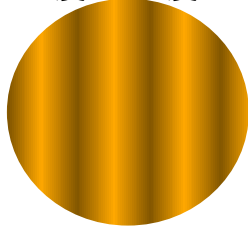
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## 背景:コントラスト感度関数 (CSF) とは

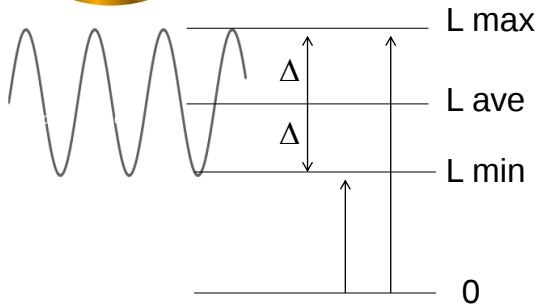
← 2度～10度 →



$$\Delta = (L_{\max} - L_{\min}) / 2$$

$$L_{\text{ave}} = (L_{\max} + L_{\min}) / 2$$

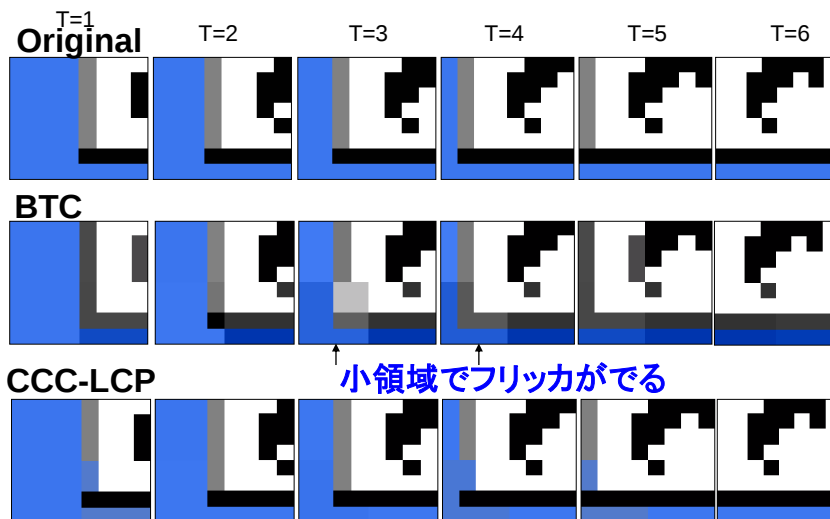
$$\text{CSF値} = L_{\text{ave}} / \Delta$$



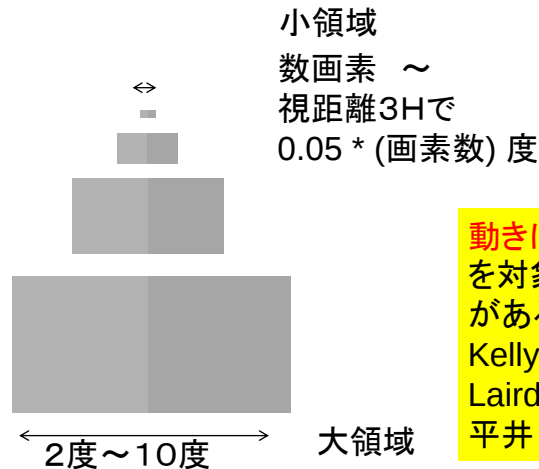
CSF値 = 1  
とは  
真っ白 VS 真っ黒

## 背景: 圧縮フリッカを考える

小領域、動き に関するCSFが必要



## 背景:コントラスト感度関数 (CSF) とは



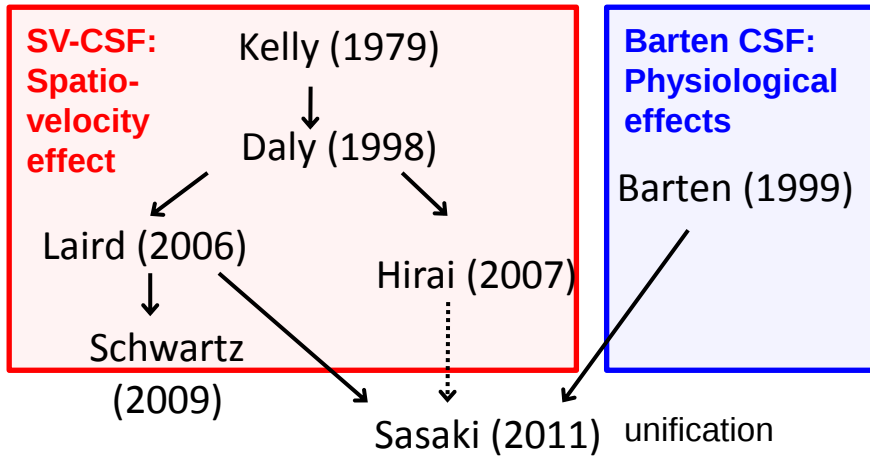
動きに関しては大領域  
を対象としたCSFのみ  
がある

Kelly & Daly SV-CSF,  
Laird SV-CSF,  
平井 SV-CSF

## Objective

- We will propose a new model on Spatio-Velocity Contrast Sensitivity Function (SV-CSF):
  - To evaluate image-processing algorithms such as block-wise memory-compression of LCD overdriving, artifact occurs in very small area. However, conventional SV-CSF model mainly targeted for large-area check of TV artifacts such as flickering and blurring. So, we need a new model.
- As a result, we will eventually have an unified treatment of two artifacts: flickering and blurring.
  - In this sense, unified treatment is a final objective.

## Historical Review of CSFs (Contrast Sensitivity Functions)



Problem: Each cannot treat both effects simultaneously.

## The Barten CSF

$$CSF(u, w) = \frac{M_{opt}(u)/k}{\sqrt{\frac{2}{T} \left( \frac{1}{X_0^2} + \frac{1}{X_{max}^2} + \frac{1}{N_{max}^2} \right) \left( \frac{1}{\eta p E} + \frac{\Phi_0}{[H_1(w)\{1 - H_2(w)F(u)\}]^2} \right)}}$$

**u: spatial frequency**  
**w: temporal frequency**

$$M_{opt}(u) = e^{-2\pi^2 \sigma^2 u^2}$$

$$\sigma = \sqrt{\sigma_0^2 + (\sigma_{ab} d)^2}$$

$$E = \frac{\pi d^2}{4} L \{ 1 - (d/9.7)^2 + (d/12.4)^4 \}$$

$$d = 5 - 3 \tanh(0.4 \log(L))$$

$$\frac{\pi}{4} D^2 = X_o^2$$

確率50%で認識できるかどうかの閾値を与える等式

$$H_n(w) = \frac{1}{\{1 + (2\pi w \tau_n)^2\}^{n/2}}$$

$$\tau_1 = \frac{\tau_{10}}{1 + 0.55 \ln \left\{ 1 + \left( 1 + \frac{D}{1} \right)^{0.6} \frac{E}{3.5} \right\}}$$

$$\tau_2 = \frac{\tau_{20}}{1 + 0.37 \ln \left\{ 1 + \left( 1 + \frac{D}{3.2} \right)^5 \frac{E}{120} \right\}}$$

$$F(u) = 1 - \sqrt{1 - e^{-(u/u_0)^2}}$$

## The Barten CSF

$$CSF(u, w) = \frac{M_{opt}(u)/k}{\sqrt{\frac{2}{T} \left( \frac{1}{X_0^2} + \frac{1}{X_{max}^2} + \frac{1}{N_{max}^2} \right) \left( \frac{1}{\eta p E} + \frac{\Phi_0}{[H_1(w)\{1-H_2(w)F(u)\}]^2} \right)}}$$

$$M_{opt}(u) = e^{-2\pi^2\sigma^2u^2}$$

$$\sigma = \sqrt{\sigma_0^2 + (\sigma_{ab}d)^2}$$

$$E = \frac{\pi d^2}{4} L \left\{ 1 - (d/9.7)^2 + (d/12.4)^4 \right\}$$

$$d = 5 - 3 \tanh(0.4 \log(L))$$

$$\frac{\pi}{4} D^2 = X_o^2$$

豊富な生理的なパラメータ

u: spatial frequency  
w: temporal frequency

$$H_n(w) = \frac{1}{\left\{ 1 + (2\pi w \tau_n)^2 \right\}^{n/2}}$$

$$\tau_1 = \frac{\tau_{10}}{1 + 0.55 \ln \left\{ 1 + \left( 1 + \frac{D}{1} \right)^{0.6} \frac{E}{3.5} \right\}}$$

$$\tau_2 = \frac{\tau_{20}}{1 + 0.37 \ln \left\{ 1 + \left( 1 + \frac{D}{3.2} \right)^5 \frac{E}{120} \right\}}$$

$$F(u) = 1 - \sqrt{1 - e^{-(u/u_0)^2}}$$

## The Hirai SV-CSF

$$svCSF_{SHIFT}(u, v_R) * C_{vd}(DIS, v)$$

$$svCSF_{SHIFT}(u, v_R) = k_{hirai} c_0 c_1 c_2 v_R (c_1 2\pi u)^2 \exp \left( -\frac{c_1 4\pi u}{u_{max}} \right)$$

$$k_{hirai} = s_1 + s_2 \left| \log \left( \frac{c_2 v_R}{3} \right) \right|^3$$

u: spatial frequency  
v: spatio-velocity

$$u_{max} = \frac{p_1}{c_2 v_R + 2}$$

$$v_R = v + c_v$$

空間速度 v がパラメータとしてある

Normalize SV-CSF by the value of v=0.

$$svCSF_{hirai} = \frac{svCSF(u, v_R)}{svCSF(u, v_R | (v = 0))}$$

## The Laird SV-CSF

$$svCSF(u, v_R) = k_{laird} c_0 c_1 c_2 v_R (c_1 2\pi u)^2 \exp\left(-\frac{c_1 4\pi u}{u_{\max}}\right)$$

$$k_{laird} = s_1 + s_2 \left| \log\left(\frac{c_2 v_R}{3}\right) \right|^3$$

$$u_{\max} = \frac{p_1}{c_2 v_R + 2}$$

$$v_R = |v - \min\{0.82 * v + 0.15, 80.0\}|$$

u: spatial frequency

v: spatio-velocity

Retinal velocity  $v_R$  is limited by 80 max.

Normalize SV-CSF by the value of  $v=0$ .

$$svCSF_{laird} = \frac{svCSF(u, v_R)}{svCSF(u, v_R | (v = 0))}$$

空間速度  $v$  がパラメータとしてある

## Three candidates as new SV-CSF

- Exploit the Barten CSF as the primary body: **CSF(u, w)**.
- Augment normalized **SV-CSF** as the modification factor.

$$CSF1 = CSF(u, w) \quad \text{Barten}$$

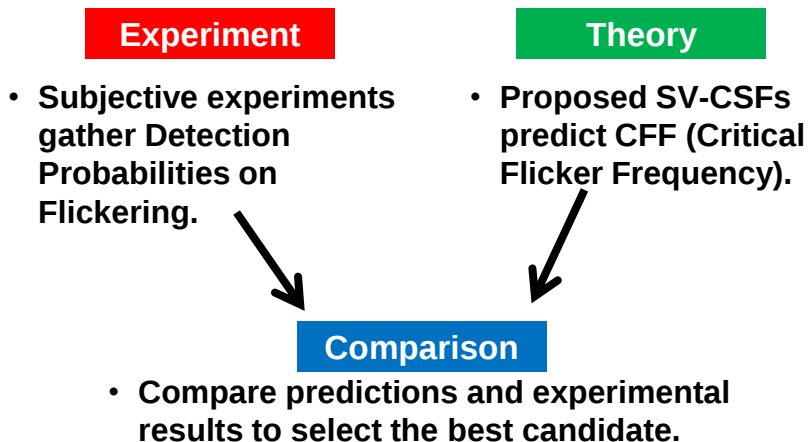
$$CSF2 = CSF(u, w) * svCSF_{hirai} \quad \text{Hirai and Barten}$$

$$CSF3 = CSF(u, w) * svCSF_{laird} \quad \text{Laird and Barten}$$

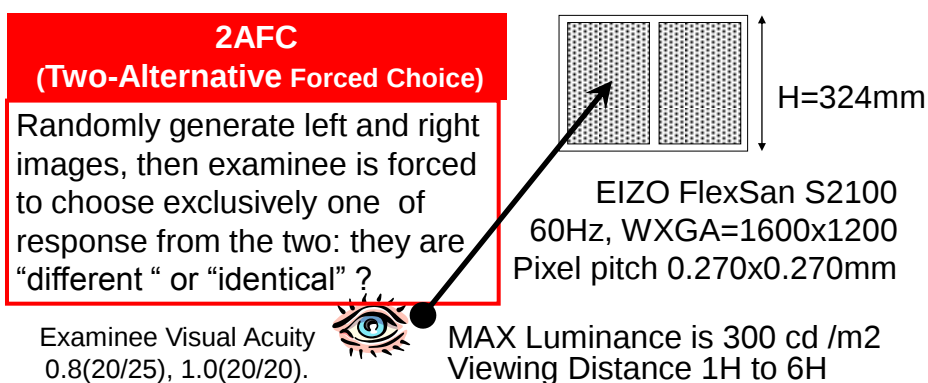
豊富な生理的なパラメータ

空間速度  $v$  がパラメータとしてある

## Strategy for Candidate Selection



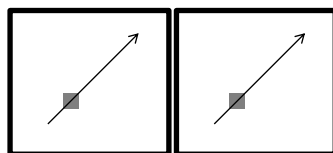
## Experimental Setup



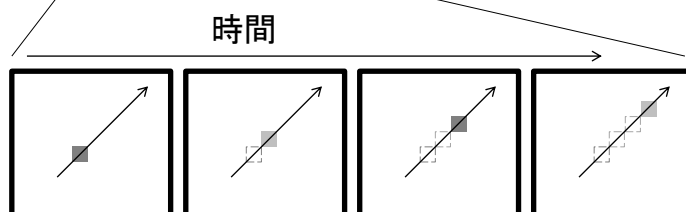
**This test gathers detection probabilities.**

## 実験：テストの対象

左右の違いを検出できるか？



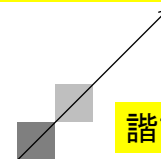
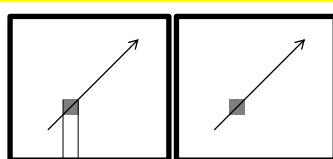
変化するテスト対象  
と変化しないテスト  
対象をランダム発生  
し、認識確率を出す



テスト対象は移動  
諧調は時分割で変化

## 実験：パラメータ

対象の移動速度  $v$  : 左上 1 [画素/フレーム]



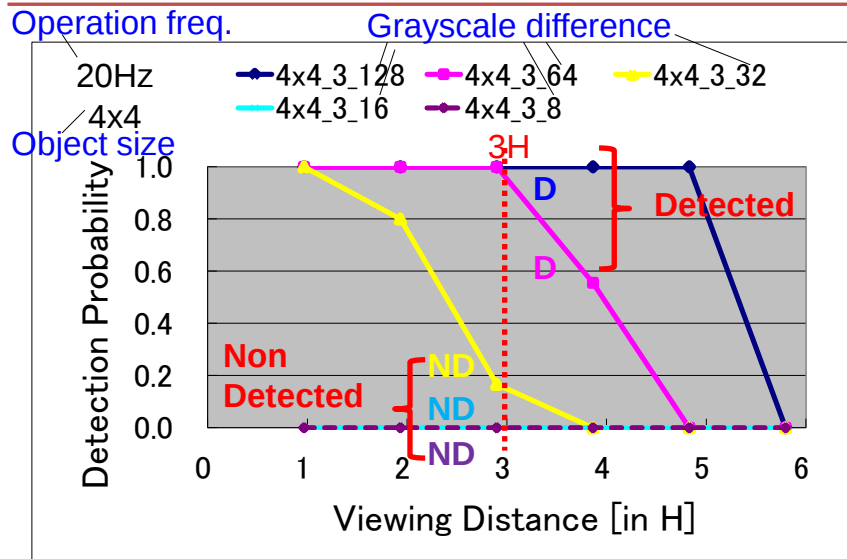
諧調差

対象の大き  
さ:  $h$   
(画素サイズ  
を単位とし  
て)

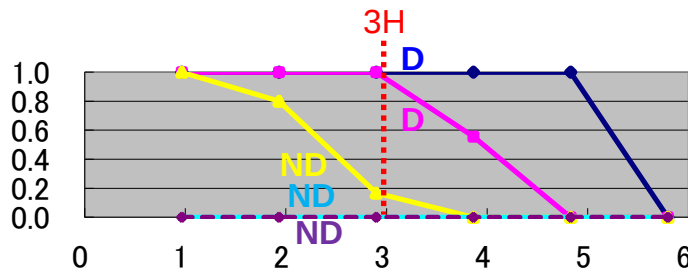
視距離  
(1H~6H)

動作周波数: 30Hz, 20Hz, 15Hz

## Experimental Result Example

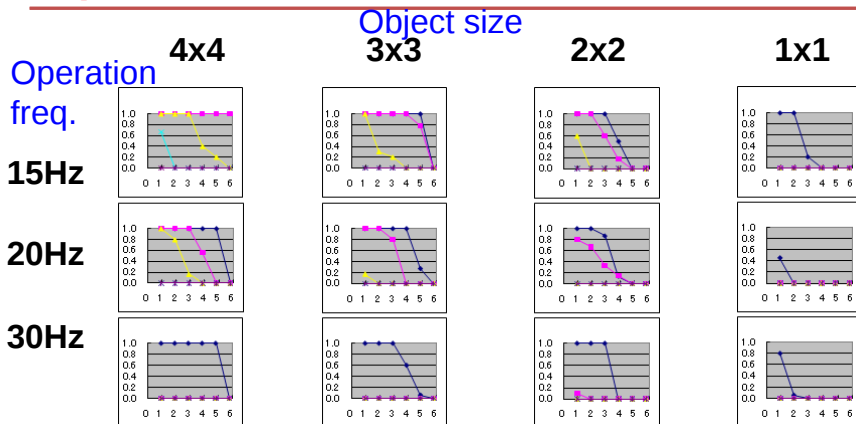


## Experimental Results Table



|                     |            |           |           |           |
|---------------------|------------|-----------|-----------|-----------|
| <b>h=4</b>          |            |           |           |           |
| <b>Difference →</b> | <b>128</b> | <b>64</b> | <b>32</b> | <b>16</b> |
| <b>Frequency ↓</b>  |            |           |           |           |
| 20Hz                | D          | D         | ND        | ND        |

## Experimental Results



| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | D  | ND |
| 20Hz                               | D   | D  | ND | ND |
| 30Hz                               | D   | ND | ND | ND |

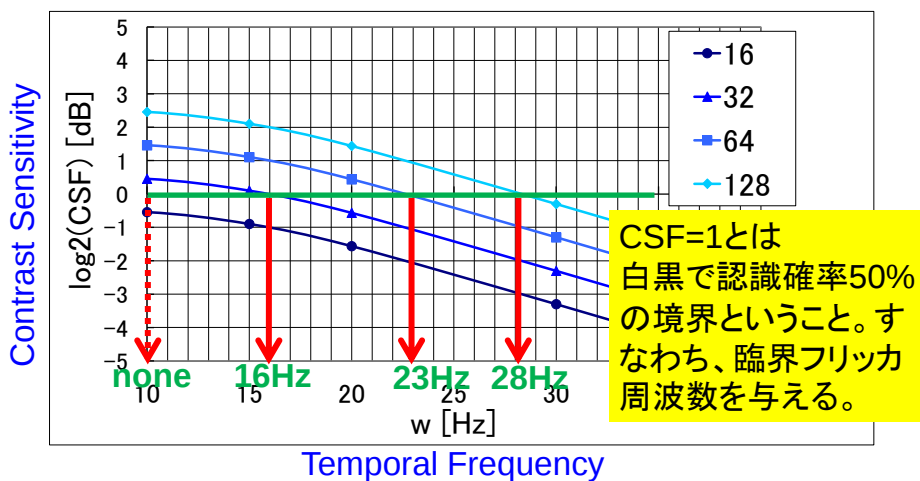
| h=3<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | ND | ND |
| 20Hz                               | D   | 50 | ND | ND |
| 30Hz                               | D   | ND | ND | ND |

| h=2<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | ND | ND |
| 20Hz                               | D   | 30 | ND | ND |
| 30Hz                               | D   | ND | ND | ND |

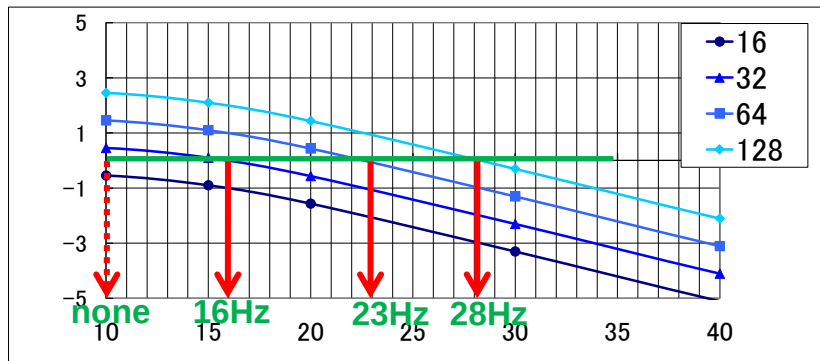
| h=1<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | 20  | ND | ND | ND |
| 20Hz                               | ND  | ND | ND | ND |
| 30Hz                               | ND  | ND | ND | ND |

## Theory: Prediction Procedure

### How to Predict CFF(Critical Flicker Frequency) by CSF



## Theory: Predicted CFF



| CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |
|---------------------------------|------|------|------|------|
| h=4                             | 28.0 | 23.0 | 16.0 | None |

## Theory: CFF Predictions

### CSF candidate

Object  
size

h=1

h=2

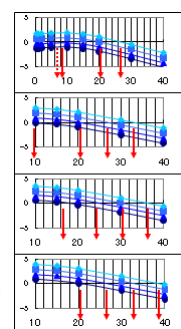
h=3

h=4

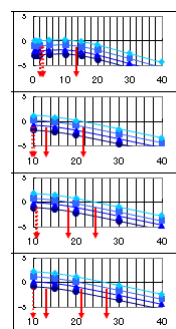
Barten

Hirai + Barten

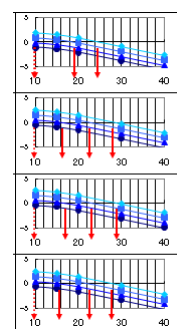
Laird + Barten



| CFF [Hz]<br>Difference →<br>h ↓ | 128 | 64 | 32 | 16   |
|---------------------------------|-----|----|----|------|
| h=1                             | 27  | 21 | 9  | None |
| h=2                             | 23  | 27 | 21 | 19   |
| h=3                             | 37  | 31 | 25 | 17   |
| h=4                             | 39  | 33 | 27 | 21   |



| CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |
|---------------------------------|------|------|------|------|
| h=1                             | 14   | None | None | None |
| h=2                             | 22   | 13.5 | None | None |
| h=3                             | 25   | 18.5 | None | None |
| h=4                             | 27.5 | 22   | 15.5 | None |



| CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |
|---------------------------------|------|------|------|------|
| h=1                             | 25.5 | 19.5 | None | None |
| h=2                             | 29.5 | 23.5 | 16.5 | None |
| h=3                             | 29.5 | 23.5 | 17.5 | None |
| h=4                             | 28.0 | 23.0 | 16.0 | None |

## Comparison Procedure: Example

| Experiments                        |     |    |    |    | Theory                          |     |    |    |    |
|------------------------------------|-----|----|----|----|---------------------------------|-----|----|----|----|
| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | CFF [Hz]<br>Difference →<br>h ↓ | 128 | 64 | 32 | 16 |
| 30Hz                               | D   | ND | ND | ND | h=4                             | 39  | 33 | 27 | 21 |

Operation freq. = 30 < 33 = CFF  
D D ND ND

| Comparison                         |     |    |    |    |
|------------------------------------|-----|----|----|----|
| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
| 30Hz                               | D   | D  | ND | ND |

disagreement

理論予測と実測の不一致

## Comparison selects CSF3 (Laird and Barten)

| Experiments                             |     |    |    |    | Theory                          |      |      |      |      |
|-----------------------------------------|-----|----|----|----|---------------------------------|------|------|------|------|
| h=4<br>Differ-<br>ence →<br>Frequency ↓ | 128 | 64 | 32 | 16 | CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |
| 15Hz                                    | D   | D  | D  | D  | h=1                             | 128  | 64   | 32   | 16   |
| 20Hz                                    | D   | D  | D  | D  | h=2                             | 128  | 64   | 32   | 16   |
| 30Hz                                    | D   | D  | D  | D  | h=3                             | 128  | 64   | 32   | 16   |
| 15Hz                                    | 20  | ND | ND | ND | h=1                             | 25.0 | 19.5 | None | None |
| 20Hz                                    | ND  | ND | ND | ND | h=2                             | 28.5 | 23.0 | 16.5 | None |
| 30Hz                                    | ND  | ND | ND | ND | h=3                             | 29.3 | 23.5 | 17.5 | None |
| 15Hz                                    | ND  | ND | ND | ND | h=4                             | 28.0 | 23.0 | 16.0 | None |

CSF1  
(Barten)

disagreement

CSF2  
(Hirai + Barten)

CSF3  
(Laird + Barten)

Best

## The best CSF3 (Laird and Barten)

$$\text{CSF3} = \text{CSF}(u, w) * \text{svCSF}_{\text{laird}}(u, v)$$

w: flickering      v: blurring

$$\text{CSF}(u, w) = \frac{M_{\text{opt}}(u) / k}{\sqrt{\frac{2}{T} \left( \frac{1}{X_0^2} + \frac{1}{X_{\text{max}}^2} + \frac{1}{N_{\text{max}}^2} \right) \left( \frac{1}{\eta p E} + \frac{\Phi_0}{[H_1(w)\{1 - H_2(w)F(u)\}]^2} \right)}}$$

**Barten CSF**

$$\text{svCSF}_{\text{laird}} = \frac{\text{svCSF}(u, v_R)}{\text{svCSF}(u, v_R | (v = 0))}$$

$$\text{svCSF}(u, v_R) = k_{\text{laird}} c_0 c_1 c_2 v_R \left( \frac{c_1 2\pi u}{c_2 v_R} \right)^2 \exp\left(-\frac{c_1 4\pi u}{c_2 v_R}\right)$$

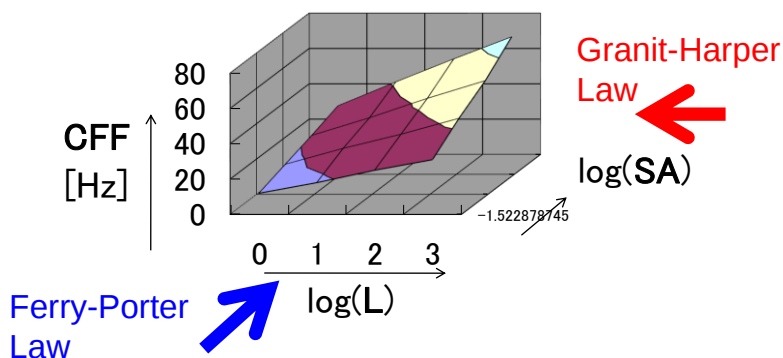
$$k_{\text{laird}} = s_1 + s_2 \left| \log\left(\frac{c_2 v_R}{3}\right) \right|^3 \quad u_{\text{max}} = \frac{p_1}{c_2 v_R + 2}$$

$$v_R = |v - \min\{0.82 * v + 0.15, 80.0\}|$$

**Laird SV-CSF**

## Discussion: a versatile applicability of CSF

The integrated Ferry-Porter Law and Granit-Harper Law.



$$\text{CFF} = 23.4 + 10.3 \log(L) + 10.7 \log(\text{SA})$$

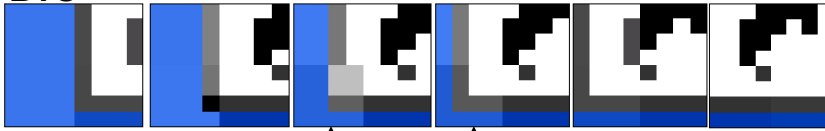
where L is a luminance, SA is subtending-angle.

## Discussion: another application of CSF

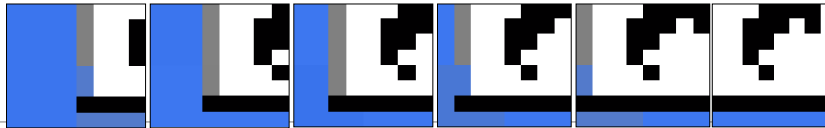
**Intuitive Design Guideline of Compression:**  
**When SA is half, 1 bit is decreased.**

$$\begin{aligned} \text{CFF} = & 29.0 + 4.06 \log_2(L) + \underset{\substack{\uparrow \\ \log_2(C) : \text{bit depth}}}{3.19 \log_2(SA) - 3.05 \log_2(C)} \\ & + 0.400 \log_2(L) \log_2(SA) - 0.133 \log_2(L) \log_2(C) + 0.0127 \{\log_2(C)\}^2 \end{aligned}$$

BTC



CCC-LCP



Cause of flicker

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## Conclusions – as a first trial to the unification

- The proposed SV-CSF treats both aspects – spatio-velocity effects and physiological parameters. So, a small-area artifact is treated.
- An unified foundation of two artifacts: flickering and blurring. That is, a phenomenon “Flickering is blurred” is formalized by the proposed SV-CSF.

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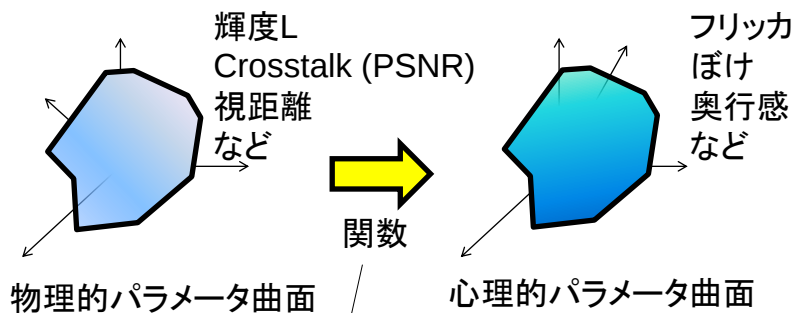
## Future Directions

- Explicit & Simpler Expression for the Normalized CSF.

$$svCSF_{laird} = \frac{svCSF(u, v_R)}{svCSF(u, v_R | (v = 0))}$$

- Chromatic SV-CSF.
- Scotopic/Mesopic CSF and SV-CSF.
- CFF macro models including other parameters such as bit depth, spatio-velocity, ...
- SV-CSF for 3D viewing: introduce the parameter “angle of convergence”? Foreground / background moving speed? Background blur? etc

## IDW'11 3D8/VHF8-4 論文



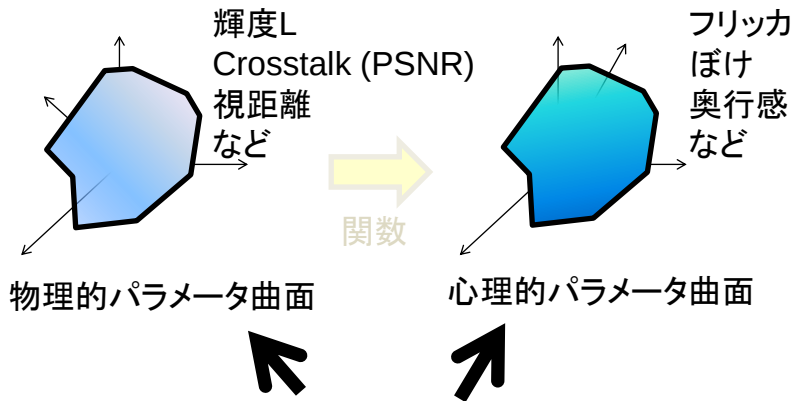
「FPDの人間工学的な評価」とはこの関数のことである。

3D8/  
VHF8 - 4

Ergonomic Assessment Theory for the  
Standardisation of 3D Displays

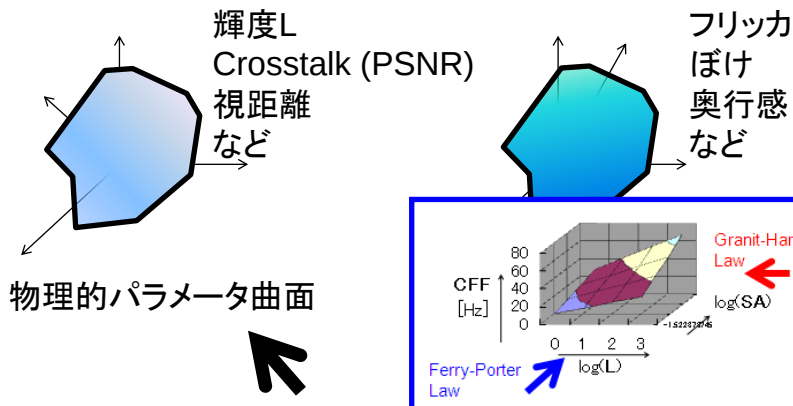
C. Kato<sup>\*,\*\*</sup>, S. Uehara<sup>\*,\*\*\*</sup>, H. Ujike<sup>\*,\*\*\*\*</sup>, Y. Hisatake<sup>\*,\*\*\*\*\*</sup>  
<sup>\*</sup>Japanese Ergonomics Nat. Committee, Japan  
<sup>\*\*</sup>Hitachi, Japan  
<sup>\*\*\*</sup>Toshiba, Japan  
<sup>\*\*\*\*</sup>AIST, Japan  
<sup>\*\*\*\*\*</sup>Toshiba Mobile Display, Japan

## Future Directions – 提案「等式としてのCSF」



$CSF(u, w) * svCSF_{laird}(u, v)$  の3D用改良  
各種パラメータを結びつける「等式」=「超曲面」

## Future Directions – 提案「等式としてのCSF」



$CSF(u, w) * svCSF_{laird}(u, v)$  の3D用改良  
各種パラメータを結びつける「等式」=「超曲面」

Thank you for your kind attention.

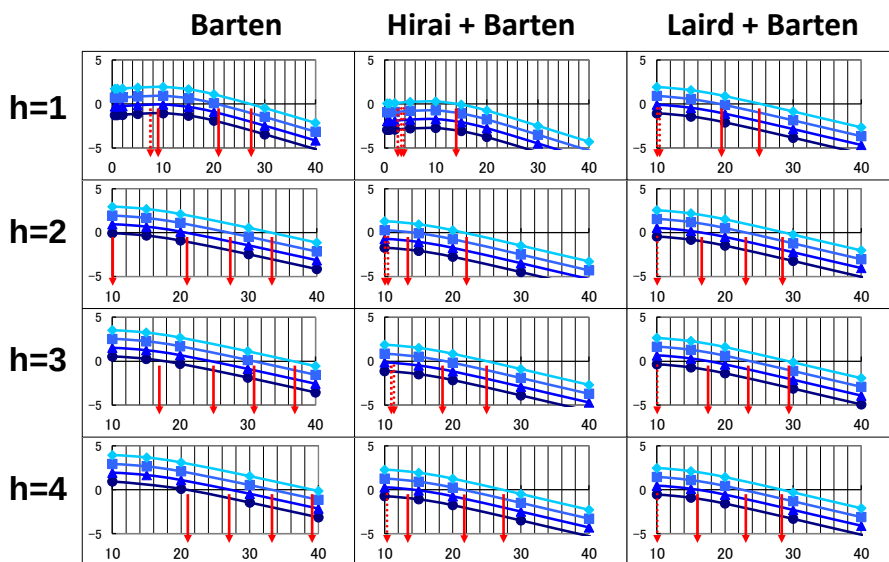


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## 補足資料

## CFF Prediction Matrix



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## Predicted CFF Summary

|                      |                                 |      |      |      |      |               |
|----------------------|---------------------------------|------|------|------|------|---------------|
| Barten               | CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   | None = no CFF |
|                      | h=1                             | 27   | 21   | 9    | None |               |
|                      | h=2                             | 33   | 27   | 21   | 10   |               |
|                      | h=3                             | 37   | 31   | 25   | 17   |               |
|                      | h=4                             | 39   | 33   | 27   | 21   |               |
| Hirai<br>+<br>Barten | CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |               |
|                      | h=1                             | 14   | None | None | None |               |
|                      | h=2                             | 22   | 13.5 | None | None |               |
|                      | h=3                             | 25   | 18.5 | None | None |               |
|                      | h=4                             | 27.5 | 22   | 13.5 | None |               |
| Laird<br>+<br>Barten | CFF [Hz]<br>Difference →<br>h ↓ | 128  | 64   | 32   | 16   |               |
|                      | h=1                             | 25.0 | 19.5 | None | None |               |
|                      | h=2                             | 28.5 | 23.0 | 16.5 | None |               |
|                      | h=3                             | 29.3 | 23.5 | 17.5 | None |               |
|                      | h=4                             | 28.0 | 23.0 | 16.0 | None |               |

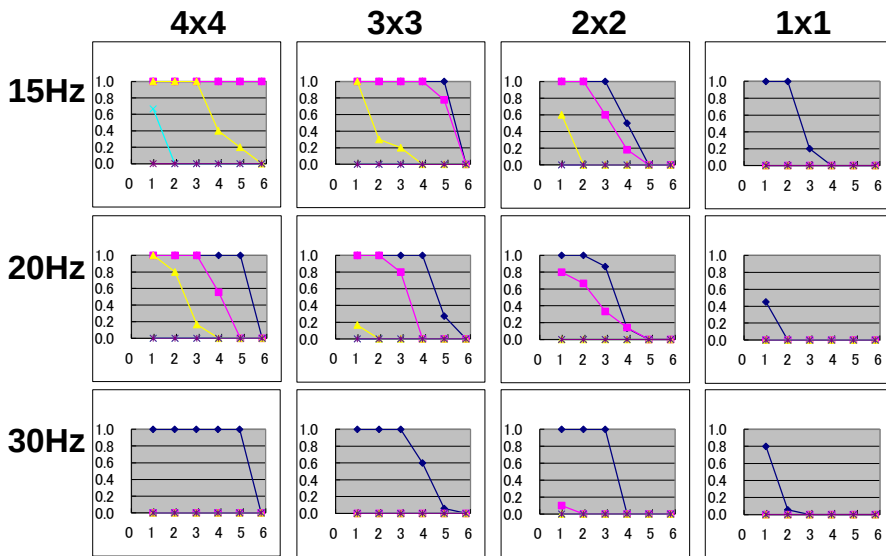
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## Experimental Results Matrix



## Experimental Results Summary

| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=3<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | D  | ND | 15Hz                               | D   | D  | ND | ND |
| 20Hz                               | D   | D  | ND | ND | 20Hz                               | D   | 50 | ND | ND |
| 30Hz                               | D   | ND | ND | ND | 30Hz                               | D   | ND | ND | ND |
| h=2<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=1<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
| 15Hz                               | D   | D  | ND | ND | 15Hz                               | 20  | ND | ND | ND |
| 20Hz                               | D   | 30 | ND | ND | 20Hz                               | ND  | ND | ND | ND |
| 30Hz                               | D   | ND | ND | ND | 30Hz                               | ND  | ND | ND | ND |

D=detected, ND=non-detected, number is a detection percent.

3H Viewing Distance

## Comparison by CSF1 (genuine Barten)

| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=3<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | D  | D  | 15Hz                               | D   | D  | D  | D  |
| 20Hz                               | D   | D  | D  | D  | 20Hz                               | D   | D  | D  | ND |
| 30Hz                               | D   | D  | ND | ND | 30Hz                               | D   | D  | ND | ND |

| h=2<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=1<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | D  | ND | 15Hz                               | D   | D  | ND | ND |
| 20Hz                               | D   | D  | D  | ND | 20Hz                               | D   | D  | ND | ND |
| 30Hz                               | D   | ND | ND | ND | 30Hz                               | ND  | ND | ND | ND |

D=detected, MD=marginally-detected, ND=non-detected

**D** disagreement

## Comparison by CSF2 (Hirai and Barten)

| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=3<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | MD | ND | 15Hz                               | D   | D  | MD | ND |
| 20Hz                               | D   | D  | ND | ND | 20Hz                               | D   | MD | ND | ND |
| 30Hz                               | MD  | ND | ND | ND | 30Hz                               | MD  | ND | ND | ND |

| h=2<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 | h=1<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | D  | ND | 15Hz                               | MD  | ND | ND | ND |
| 20Hz                               | MD  | D  | D  | ND | 20Hz                               | ND  | ND | ND | ND |
| 30Hz                               | ND  | ND | ND | ND | 30Hz                               | ND  | ND | ND | ND |

D=detected, MD=marginally-detected, ND=non-detected

**D** disagreement

## Comparison by CSF3 (Laird and Barten)

| h=4<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | MD | ND |
| 20Hz                               | D   | MD | ND | ND |
| 30Hz                               | MD  | ND | ND | ND |

| h=3<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | MD | ND |
| 20Hz                               | D   | MD | ND | ND |
| 30Hz                               | MD  | ND | ND | ND |

| h=2<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | D   | D  | MD | ND |
| 20Hz                               | D   | MD | ND | ND |
| 30Hz                               | MD  | ND | ND | ND |

| h=1<br>Difference →<br>Frequency ↓ | 128 | 64 | 32 | 16 |
|------------------------------------|-----|----|----|----|
| 15Hz                               | MD  | ND | ND | ND |
| 20Hz                               | ND  | ND | ND | ND |
| 30Hz                               | ND  | ND | ND | ND |

D=detected, MD=marginally-detected, ND=non-detected



disagreement